

**The Internal Structure of
Predicates and Names
with an
Analysis of Reasoning about Processes**

The Semantic Foundations of Logic

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The Semantic Foundations of Logic

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Classical Logic

Dependence Logic

Relatedness Logic

Predicate Logics with Non-Referring Names

A General Framework

The Modal Logic S5

The Many-Valued Logic L_3

Intuitionism

Translations Between Logics

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